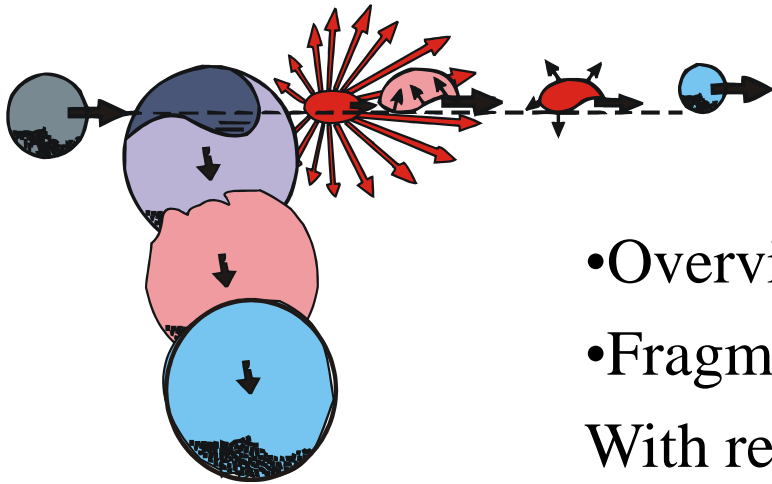


# Projectile Fragmentation

modern route to exotic nuclei

D.J. Morrissey, NSCL & Dept. of Chemistry,  
Michigan State Univ.



- Overview of Reaction Mechanism
- Fragment Separators

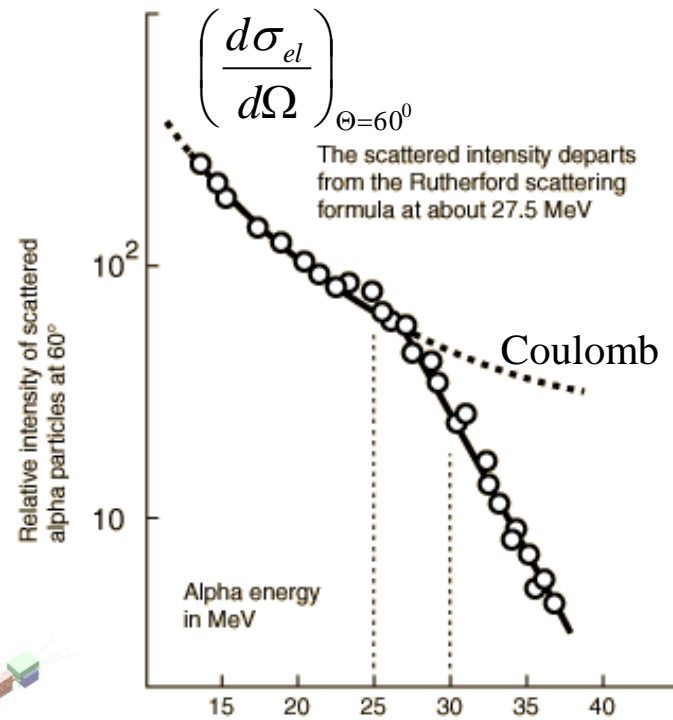
With references and estimates of typical values

# Why the fast beams ?

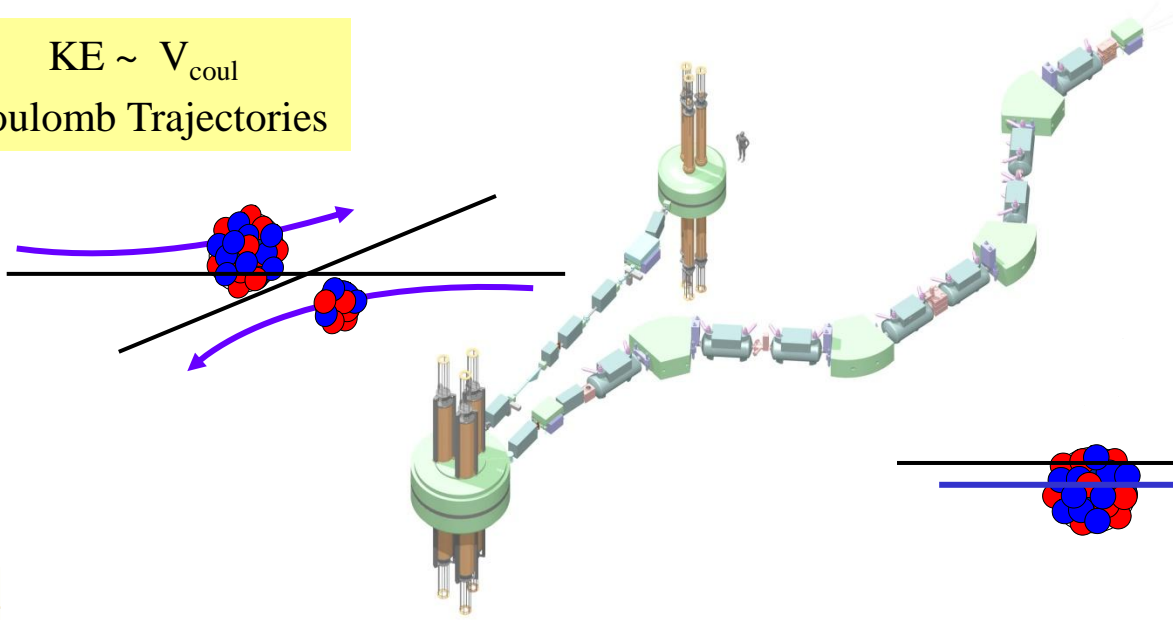
## (a) Rutherford Scattering

$$\frac{dS}{d \cos q} = \frac{\rho}{2} z^2 Z^2 a^2 \frac{\hbar c}{e KE} \frac{1}{(1 - \cos q)^2}$$

e.g., He + Pb, Eisberg and Porter, Rev. Mod. Phys. **33**(1961)190



KE ~ V<sub>coul</sub>  
Coulomb Trajectories

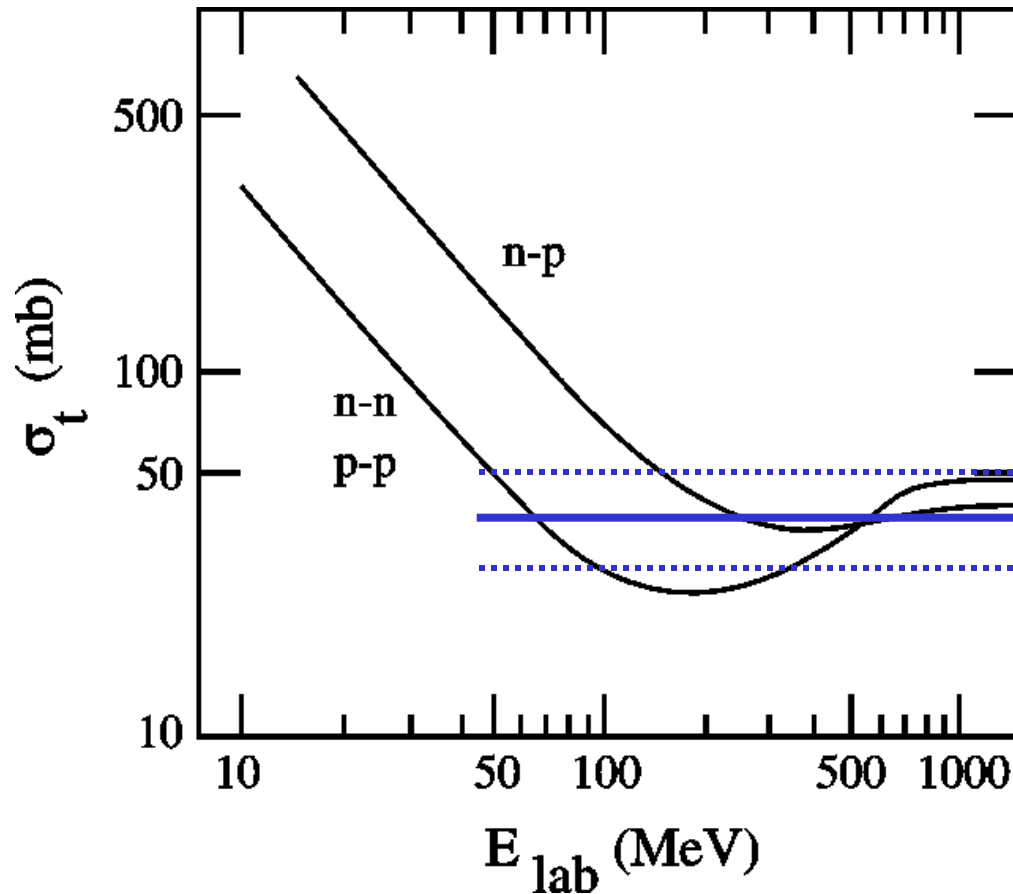


KE >> V<sub>coul</sub>  
~ Straight-line Trajectories



# Why the fast beams ? (b) geometrical cross sections

## Nucleon-nucleon scattering Cross sections



Mean free path,  $\lambda$ :  
 $\lambda = 1 / (\rho \sigma)$

$$\rho = 0.15 \text{ fm}^{-3}$$

$$\sigma \sim 40 \text{ mb} \quad (\pm 25\%)$$

$$\lambda = 1.7 \text{ fm} < R_{\text{nucleus}}$$



# Empirical Production Cross Sections

## Target Fragments:

G. Rudstam,

Z. Naturforsch. 21a (1966) 1027

## Cosmic Rays:

R. Silverberg and C.H. Tsao,

Ap. J. Suppl. 25 (1973) 313, 58 (1985) 873

## Unified Systematics:

K. Suemmerer, et al., EPAX

Phys. Rev. C42 (1990) 2546

B.Blank & KS, EPAX2

Phys. Rev C61 (2000) 034607

R. Pfaff, et al.,

Phys. Rev. C53 (1996) 1753

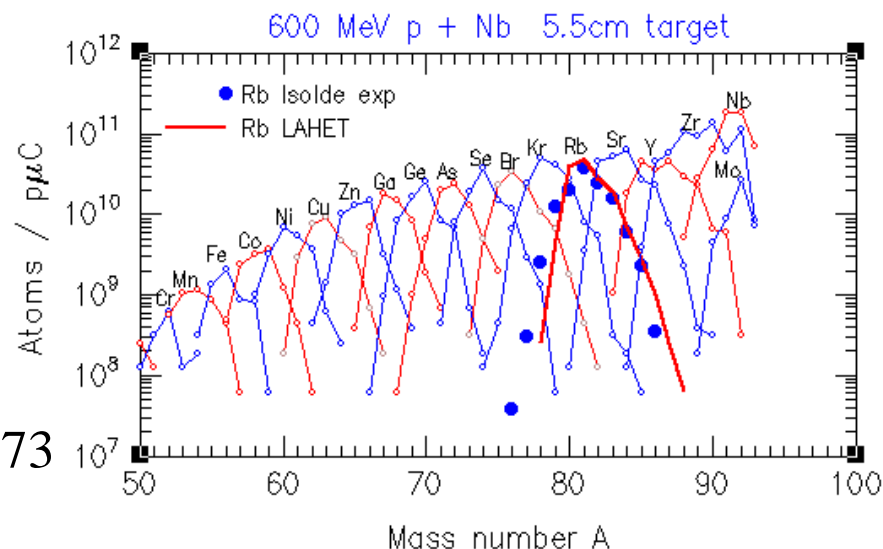
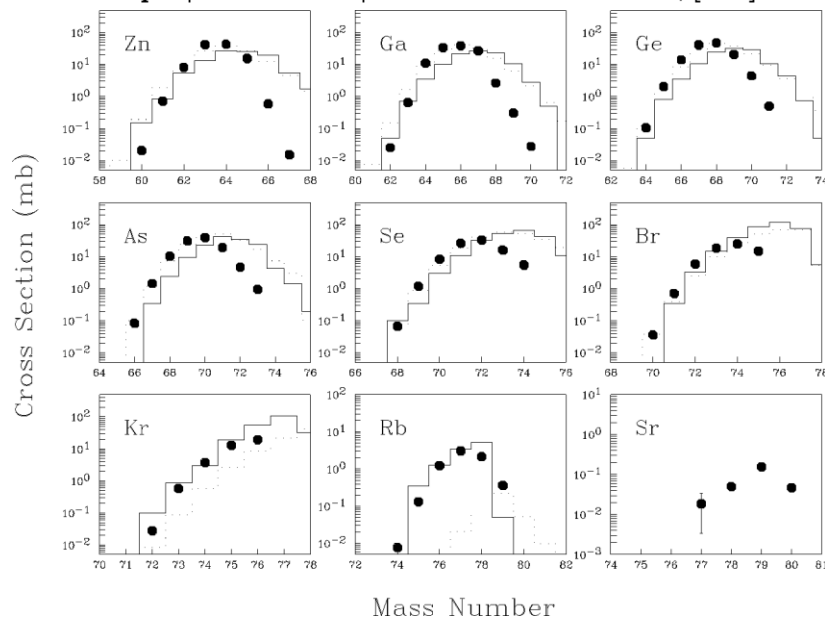


Fig. 11.13: LAHET prediction (solid curves) for 600 MeV p+Nb are compared to experimental data for Rb isotopes (solid blue circles) obtained from ISOLDE at CERN, [RAB8].



Mass Number



# Aside: Reaction Models

## Intranuclear Cascade:

VEGAS by K. Chen, Z. Fraenkel, et al.,  
Phys. Rev. 166 (1968) 949

ISABEL by Yariv and Fraenkel,  
Phys. Rev. C20 (1979) 2227

INCL4 by Cugnon, et al.  
Phys. Rev. C66 (2002) 044615

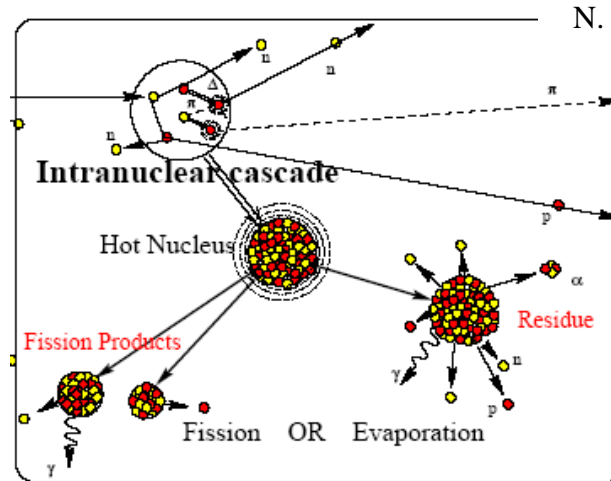
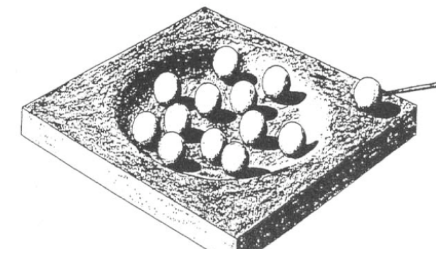
## “Macroscopic”

Abrasion/Ablation by J.D. Bowman,  
W.J. Swiatecki, and C.F. Tsang, LBL-2908

FIREBALL by J. Gossett, et al.,  
Phys. Rev. C16 (1977) 2227

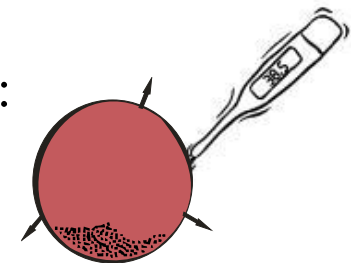
FIRESTREAK by W.D. Myers,  
Nucl. Phys. A296 (1978) 177

ABRABLA by J.-J. Gaimard, et al.,  
Nucl. Phys. A531 (1991) 709.



N. Bohr, Nature 137 (1936) 351

Unresolved problem:  
What's the  $E^*$  ?

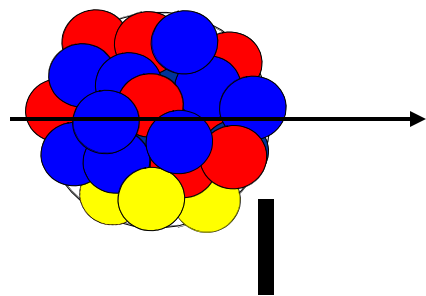


*K-H Schmidt, 2001*

[www-wnt.gsi.de/kschmidt/thermome.htm](http://www-wnt.gsi.de/kschmidt/thermome.htm)

djm Exotic Beam SumSch July/11

# Momentum Distribution, (a) centroids



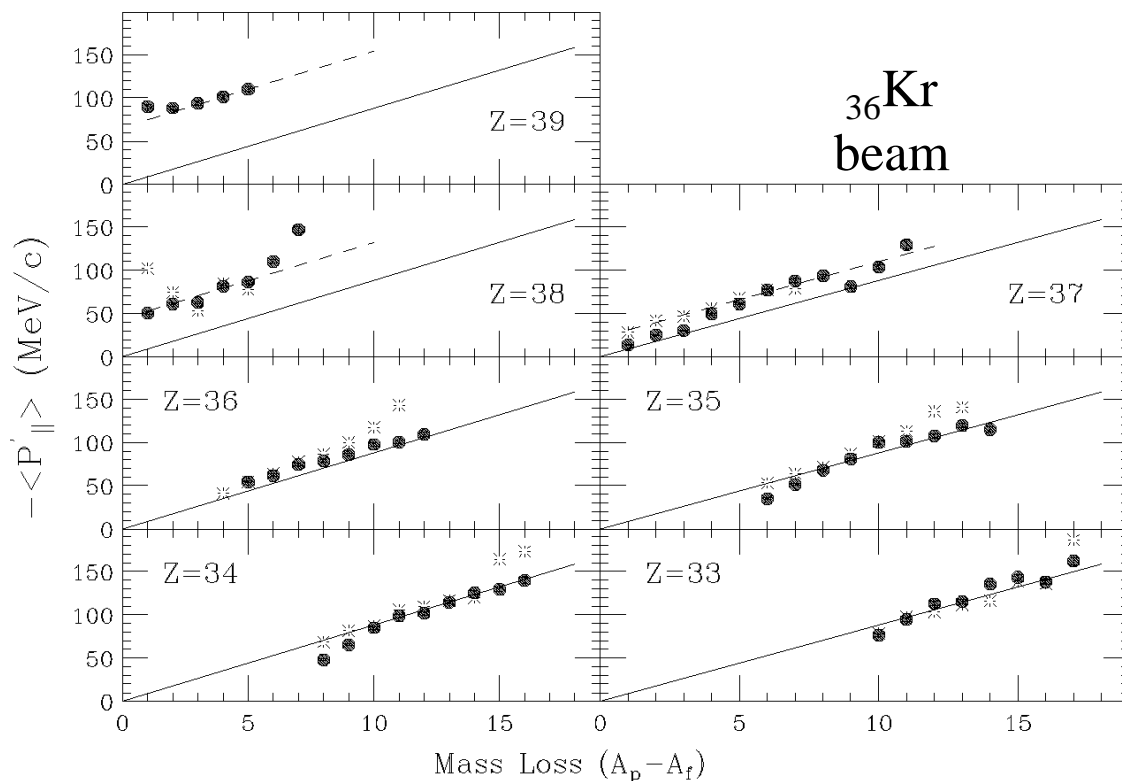
Removal of bound nucleons:

$$q_i c \sim \Delta E_i (\gamma + 1) / \beta \gamma$$

$$-\langle P_{\parallel} \rangle \sim 8 \Delta A \text{ (MeV/c)}$$

Pickup of target nucleons:

$$\langle p_f \rangle = [ (A_f - \Delta A_t) P_B / A_B + \Delta A_t p_{\text{Fermi}} ]$$



$^{86}\text{Kr} + ^9\text{Be}$  data:

R. Pfaff, et al., *Phys. Rev.* **C51** (1995) 1348

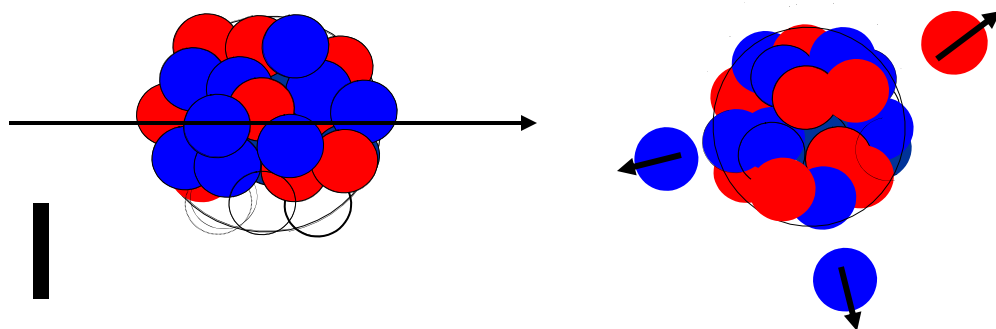
Models:

DJM, *Phys. Rev.* **C39** (1989) 460

G.A. Souliotis, et al., *Phys. Rev.* **C46** (1992) 1383



# Momentum Distribution, (b) de-excitation widths



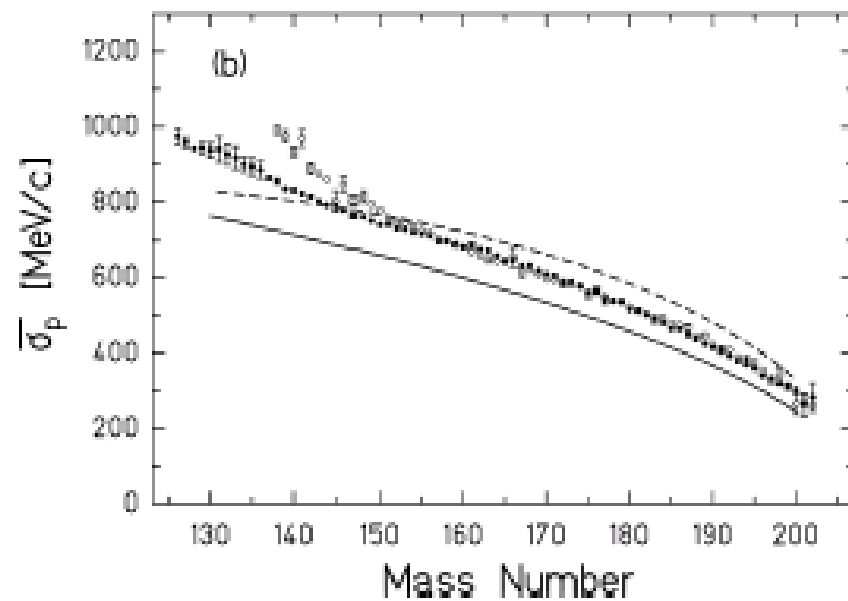
## Isotropic Recoils

- from initial process [Goldhaber]
- from de-excitation [evaporation]

$$\sigma_{\parallel}^2 = \sigma_0^2 [ (A_B - A_f) A_f / (A_B - 1) ]$$

$$\sigma_{\parallel}^2 \sim \Delta A (A_f / (A_B - 1))$$

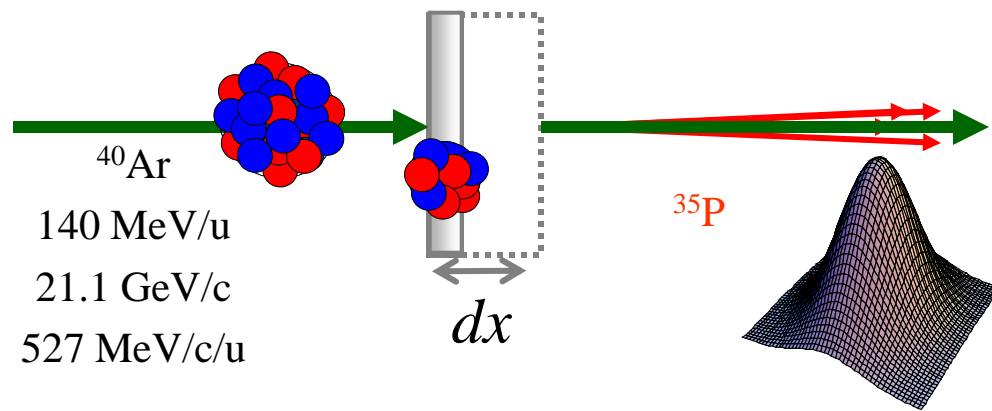
$$\sigma_{\parallel}^2 \sim \Delta A$$



$^{208}\text{Pb} + ^1\text{H}$  (open),  $^{208}\text{Pb} + ^2\text{H}$  data (full symbols):  
*T. Enqvist, et al., Nucl. Phys. A703 (2002) 435*  
 dashed: Goldhaber, *Phys.Lett. B53 (1974) 306*  
 solid: DJM, *Phys. Rev. C39 (1989) 460*



# Cartoon of Projectile Fragmentation



$S(p_{\perp}, p_{\parallel}) \gg$  gaussian

$p_{\parallel} \gg 18,000 \text{ MeV/c}$

$\gg 520 \text{ MeV/c/u}$

( Strong dependence on  $dx$  )

$S_{\parallel} \gg 300 \text{ MeV/c}$  (1.7% of  $p_{\parallel}$ )

( Weak dependence on  $dx$  )

Fraction converted,  $f$

$$f = \frac{\text{Production Rate}}{\text{Beam Flux}} = \frac{R}{\Phi} = N_0 \sigma_{rxn}$$

$$f = \left( \frac{\rho_{\text{tgt}} N_A}{A W_{\text{tgt}}} dx \right) \sigma_{rxn}$$

$$f \approx \left( \frac{2 (\text{g/cm}^3) 6 \times 10^{23} (\text{/mole})}{9 (\text{g/mole})} 0.1 (\text{cm}) \right) 10^{-24} \left( \frac{\text{cm}^2}{\text{barn}} \right)$$

$$f \approx 0.013 / \text{barn}$$

(e.g.,  $^{35}\text{P}$   $\sigma \sim 0.002 \text{ barn}$ ,  $f \sim 10^{-5}$ )





# Thumbnail of Projectile Fragmentation Facilities

First Experiments – LBL BEVALAC [late 70's]

First Generation, used existing device: – LISE @ GANIL

Second Generation, construct specific device:

A1200 @ NSCL,  $K=K_{\text{accel}}$   
superconducting, begins beamlines

FRS @ GSI,  $K=K_{\text{accel}}$   
'full acceptance', begins beamlines

RIPS @ RIKEN,  $K=1.65 K_{\text{accel}}$   
'large acceptance'

Lithium,  $A/q$   
 $11/3$  vs.  $7/3 \Rightarrow 1.6$   
Tin,  
 $132/50$  vs.  $118/50 \Rightarrow 1.1$   
  
 $K1200$  accel  $\Rightarrow$   $A1900$  sep.

Third Generation, construct improved high-resolution device:

LISE3 @ GANIL, post selection in Wien filter

A1900 @ NSCL,  $K=1.6 K_{\text{accel}}$  superconducting, begins beamlines

Fourth Generation – preselection before high resolution separator:

A1900 & S800 beamline – recently tested

bigRIPS @ RIKEN – just finished

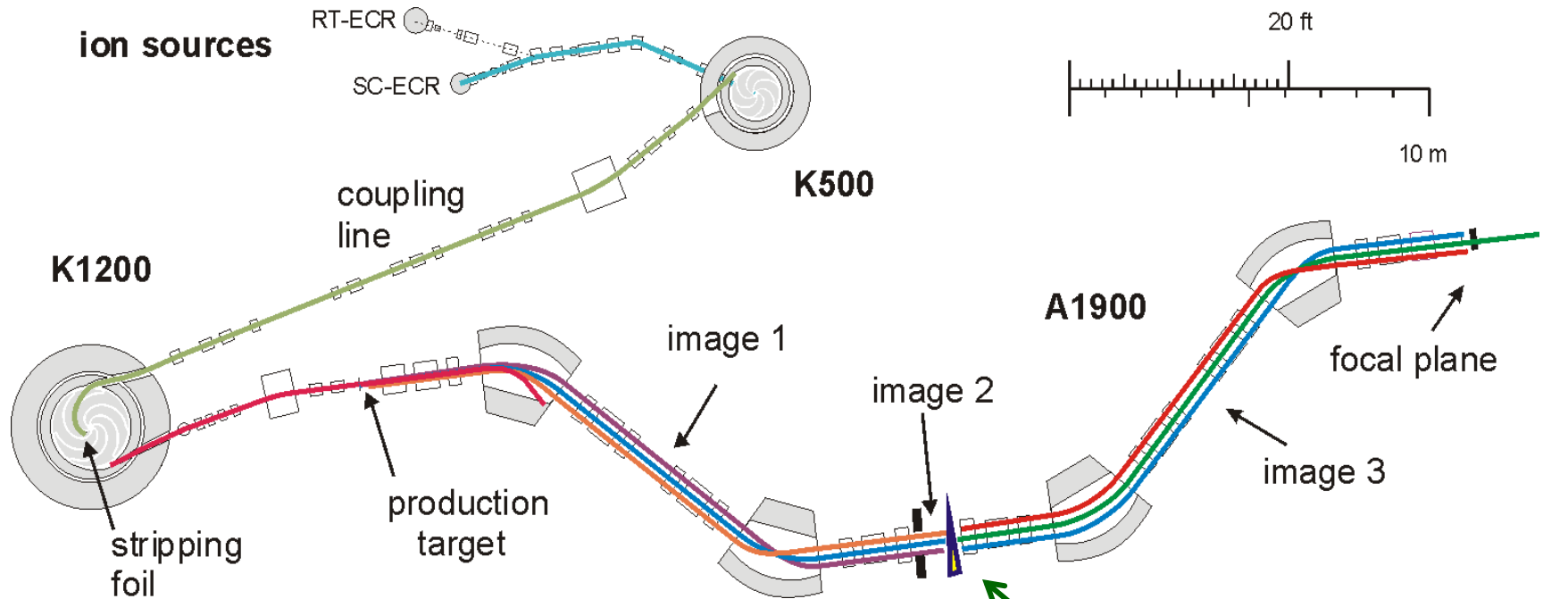
superFRS @ GSI – in design

A2400 @ F.RIB – in design



# Production in 0° Spectrometer

Example:  $^{86}\text{Kr} \rightarrow ^{78}_{28}\text{Ni}_{50}$  (doubly magic ...)



$$d\Omega = 8 \text{ msr}$$

$$\Delta p/p = 5\%$$

Wedge location

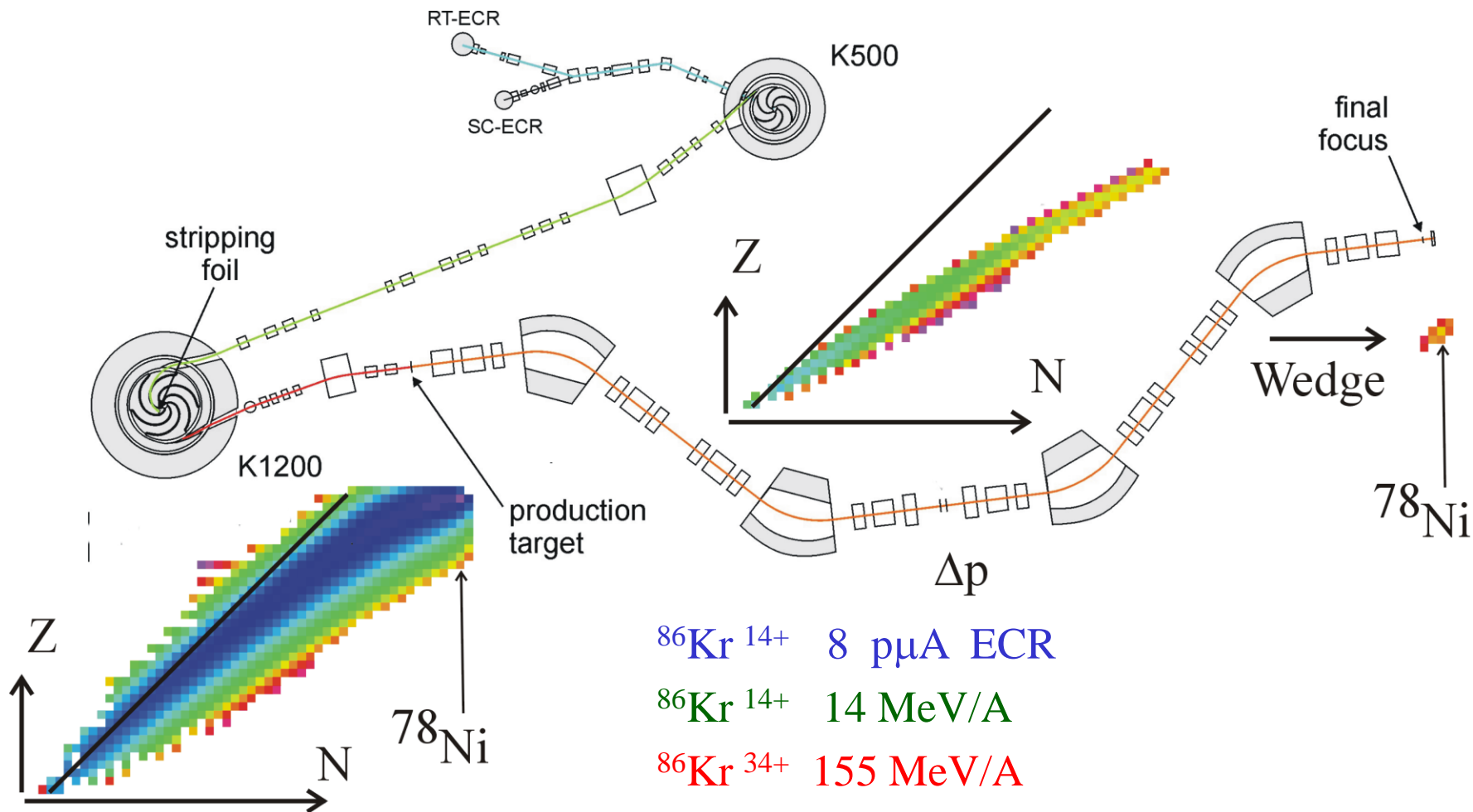
Dispersion = 5 cm/%

Resolution = 2500 p/ $\Delta p$



# Fragment Separation Example

$^{86}\text{Kr} \rightarrow ^{78}\text{Ni}$ , battle conditions



$^{86}\text{Kr}^{14+}$  8  $\mu\text{A}$  ECR

$^{86}\text{Kr}^{14+}$  14 MeV/A

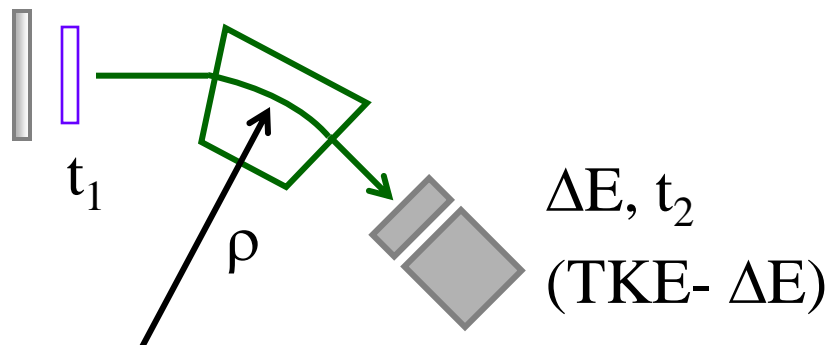
$^{86}\text{Kr}^{34+}$  155 MeV/A

→ 65% of the  $^{78}\text{Ni}$  is transmitted

Max (NSCL): 100 pA (1.3 kW power)  $\sim 10^{-2}$ /s

PRL 94(2005) 112501: 15 pA (0.2kW)

# Particle Identification Concept, $A_Z^{q+}$



## Magnetic Rigidity

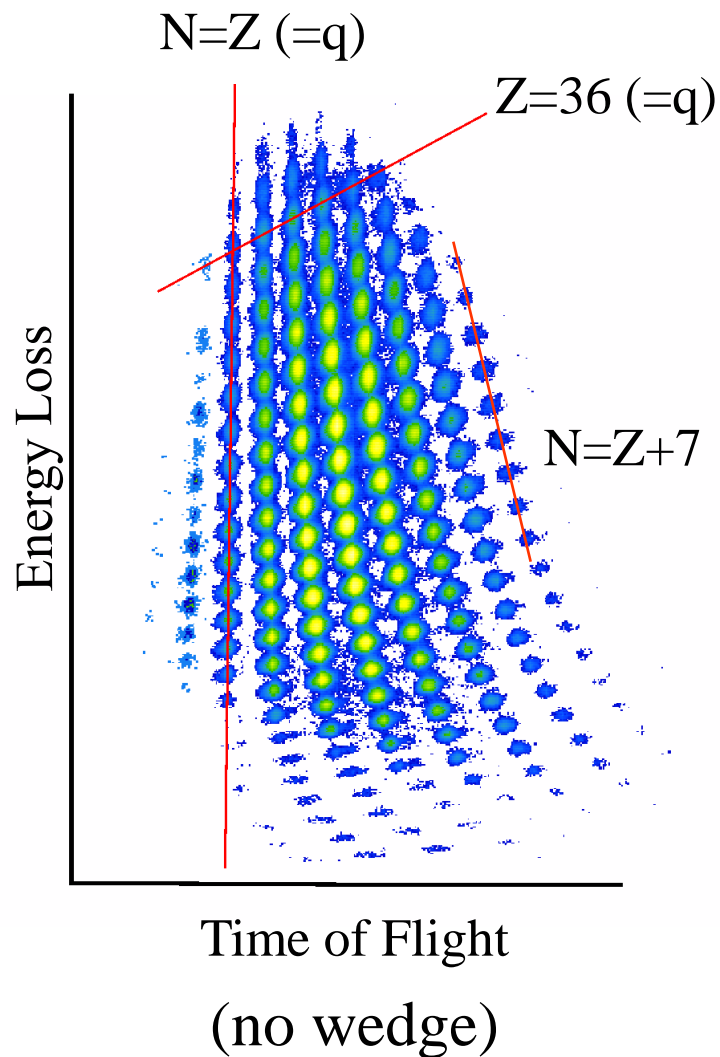
$$B\rho = p/q = m \beta\gamma / q$$

$$\beta \propto 1/(t_2 - t_1)$$

$$Z \propto \text{Sqrt}(\Delta E (\gamma + 1))$$

$$q \propto \text{TKE} \beta \gamma / B\rho (\gamma - 1)$$

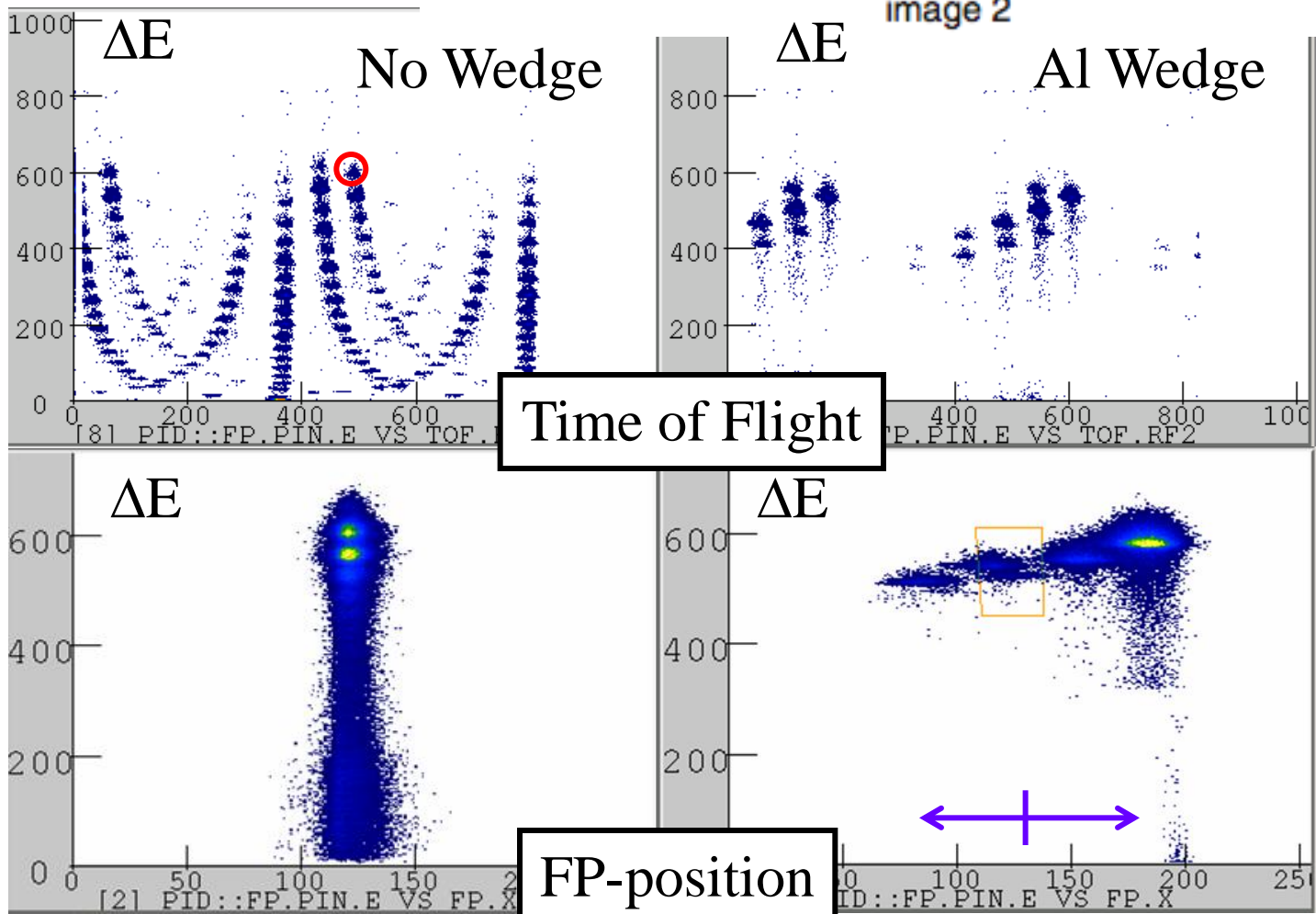
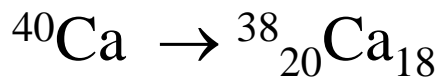
$$A = q B\rho / \beta \gamma$$



**S** Auxiliary measurement: positions/angles

# Details: Wedge Effect?

Example:



$B\rho_{1,2}$   
=  $B\rho_{3,4}$

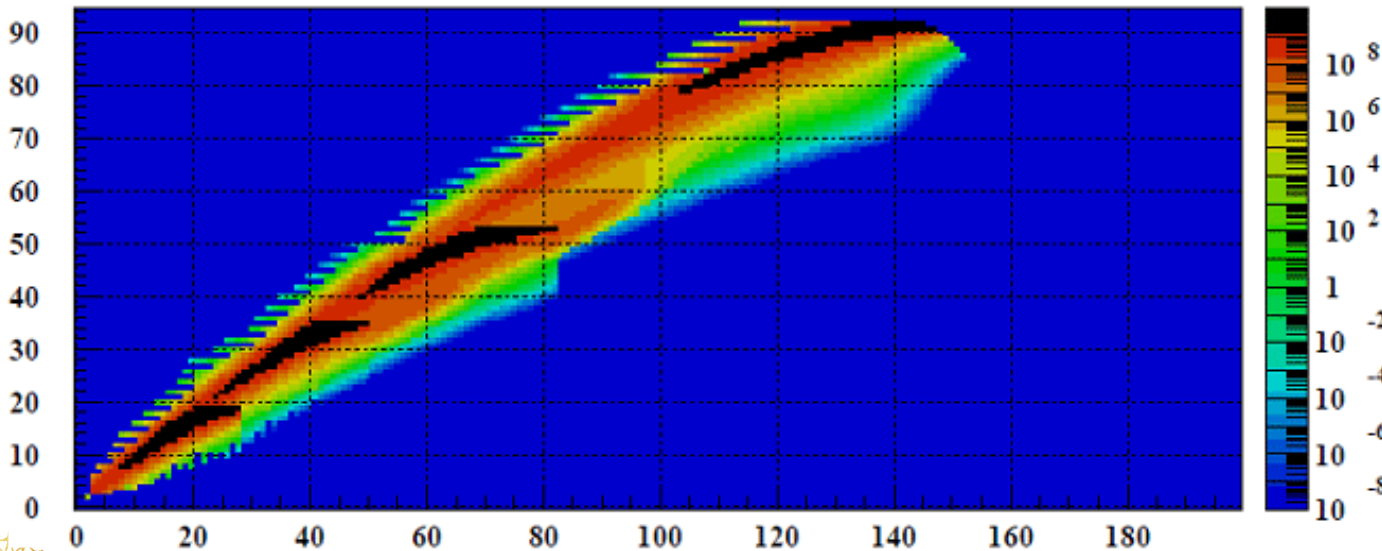
$B\rho_{1,2}$   
>  $B\rho_{3,4}$



**S**

# Summary

- Simple nuclear reactions provide a broad range of nuclei
- General features of the reactions are well-known but some details are not
- Projectile fragments are produced at nearly the speed of light
- Projectile fragments:
  - Rapid physical separation of fragment in a magnetic system
  - Requires:  $Z$ ,  $A$ , and  $q$  identification/separation in  $0^\circ$  spectrometer



A few beams or targets produce a broad range of products

<http://www.rarf.riken.go.jp/UsersGuide/BigRIPS/intensity.html>

