

U.S. Particle Accelerator School

Education in Beam Physics and Accelerator Technology

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Mesh Refinement in Field Solvers

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Outline

- Why mesh refinement?
- Potential issues
- Electrostatic mesh refinement
 - spurious self-force example
 - spurious self-force mitigation
 - application to the modeling of HCX injector
- Electromagnetic mesh refinement
 - spurious reflection of waves
 - spurious reflection of waves mitigation
 - Application to the modeling beam-induced plasma wake
- Special mesh refinement for particle emission
- Summary





Coupling of AMR to PIC: issues

Mesh refinement implies:

- → jump of resolution at coarse-fine interface,
- → some procedure for coupling the solutions at the interface.



Consequences:

- loss of symmetry: self-force,
- loss of conservation laws,
- EM: waves reflection.



Refinement levels



- 1. solve on coarse grid,
- 2. interpolate on fine grid boundaries,
- 3. solve on fine grid.



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Test using script test1partin1patch.py:

• Run with l_mr=0.

One charged macroparticle in a box with metallic BC





Test using script test1partin1patch.py:

• Run with I_mr=0.

The macroparticle is attracted by its image from the closest metallic wall.





Test using script test1partin1patch.py:

• Run with I_mr=0.

We apply specular reflection at the boundary.





Test using script test1partin1patch.py:

• Run with I_mr=0.





Test using script test1partin1patch.py:

• Run with l_mr=1.

Now add a refinement patch.







Spurious self-force: magnitude map

Map of spurious self-force as a function of particle position in refinement patch







- 3 -solve on fine grid,
- 4 disregard fine grid solution close to edge when gathering force onto particles.

Thickness of buffer region provides user control of relative magnitude of spurious force.



Test using script test1partin1patch.py:

• Run with I_mr=1, ntransit=0.

No buffer: particle trapped in patch.



Example with 2 and 4 guard cells buffer region





Test using script test1partin1patch.py:

• Run with I_mr=1, ntransit=1.

With buffer: no more trapping

Example with 2 and 4 guard cells buffer region







Test using script test1partin1patch.py:

• Run with I_mr=1, ntransit=2.

With buffer: no more trapping 4 guard cells better than 2



Example with 2 and 4 guard cells buffer region



Buffer region is very effective.



Electrostatic AMR PIC example: HCX



The Heavy Ion Fusion Virtual National Laboratory





Electrostatic AMR PIC example: HCX





Electrostatic AMR PIC example: HCX





Modeling of source critical - determines initial shape of beam.

Axisymmetric (RZ) time-dependent simulations.



A fairly high resolution is needed to reach convergence

Run	Grid size	Nb particles
Low res.	56x640	~1M
Medium res.	112x1280	~4M
High res.	224x2560	~16M
Very High res.	448x5120	~64M





First MR attempt - 1 MR block surrounding emitter.



0.2 Z(m)

0.1

0.3

N	Run	Grid size	Nb particles
14	Low res.	56x640	~1M
	Medium res.	112x1280	~4M
₩# f ###	High res.	224x2560	~16M
	Medium res. + MR	112x1280	~4M
0.4			

Refining around the emitter

area is enough to recover

emittance from converged

high-resolution case.



0.2 ∟ 0.0

First MR attempt - 1 MR block surrounding emitter (2).

However, it is not enough for recovering details of distribution.





Full adaptive mesh refinement implementation --speedup from AMR: x10





Full adaptive mesh refinement implementation --speedup from AMR: x10

Full AMR enable recovery of details of distribution.





Example of AMR at edge of beam



Test using script testxy_amr.py:

- Run with case='lowres', then 'highres' and 'AMR'.
- Observe how using AMR enables accurate simulation at reduced CPU cost.



Summary of electrostatic AMR-PIC

- Simple method for electrostatic AMR-PIC was presented.
- Buffer region mitigates spurious self-force effect very effectively.
- Speedups of x10 demonstrated on simulation of injector.
- Alternate methods such as multipole expansions have other advantages & drawbacks.



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1-D FDTD EM wave equation

• We consider 1d wave equation (natural units)

$$\frac{\partial E}{\partial t} = \frac{\partial B}{\partial x}; \quad \frac{\partial B}{\partial t} = \frac{\partial E}{\partial x}$$

 staggered on a regular space time grid using finitedifference time-domain (FDTD) centered scheme

$$\frac{E_{j}^{i+1} - E_{j}^{i}}{\delta t} = \frac{B_{j+1/2}^{i+1/2} - B_{j-1/2}^{i+1/2}}{\delta x}$$
$$\frac{B_{j+1/2}^{i+1/2} - B_{j+1/2}^{i-1/2}}{\delta t} = \frac{E_{j+1}^{i} - E_{j}^{i}}{\delta x}$$





1-D MR-EM: space refinement uncentered finite-difference





1-D MR-EM: space refinement centered finite-difference





1-D MR-EM: coefficients of spurious reflection



 $\lambda \leq \lambda_{Nyquist}$ of coarse grid are reflected with amplification of total energy!



Warp & WarpX's Electromagnetic MR use PML and substitution to prevent reflections

- Termination of patches with Perfectly Matched Layers (PML) to avoid spurious reflections
- Buffer zone used for mitigating spurious self-force





MR procedure is recursive, accommodating an arbitrary number of levels

Example with two levels of refinement





Test with single particle

Single particle orbiting around an external magnetic field, emitting synchrotron radiation



Validation on charged particle beam breathing

Electron Gaussian distribution with inward initial radial velocity on top of static proton dist.



Electron beam contraction/expansion depends on resolution.



1.0

1e-7

Laser injection with mesh refinement test



Laser generated with antenna.



Example: simulation of beam-induced plasma wake



Slab XZ simulations



Warp

Example: simulation of beam-induced plasma wake



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•

Speedup x10 in 3D (using the same time steps for all refinement levels).

Warp

First simulations of plasma accelerators with MR patch – 2-D





First simulations of plasma accelerators with MR patch – 3-D

3-D Laser driven 10.0 7.5 1011 5.0 2.5 z (μm) E 0.0 0 -2.5-5.0 -10^{11} -7.5 -10.0_20 -15 15 -10-55 10 2 0 y (µm) 12 nx32 emittance (pi um urad) 10 nx32 mr nx64 8 6 4 2 0 -20 0 20 40 60 80 100 120 z (um)

Simulations with small MR patch recover results using finer grid over the entire box.







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Movies of 3D runs



Movies by Maxence Thevenet





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3-D WARP simulation of HCX showed beam head scrapping







Test: 1-D time-dependent modeling of ion diode





Test: 1D time-dependent modeling of ion diode (algo 1)





Unphysical oscillation related to Nb particles injected/time step (N_i)





Cure: derive voltage history numerically





Cure #2: apply irregular gridded patch around emitter.





Cure #3: apply regularly gridded patch following front.





Extension to three dimensions



- Without MR, WARP predicts overshoot
- Run with MR predicts very sharp risetime (not square due to erosion)



Test of MR patch on modeling of STS500 Experiment.





Pierce diode: exercise

- (1) Open Pierce_diode_mrinj.py. Run with w3d.inj_nz = 0, 10, 20 and 100.
- 2 Observe convergence of voltage at t=0 toward 0. Notice very small dz required!





AMR-PIC summary

- Mesh refinement (static or adaptive) can reduce simulation time by several.
- Care is needed to avoid spurious effects (spurious charge & reflections).
- Warp implementation has validated methods, but maintenance is lacking sufficient manpower:
 - \rightarrow To be used with great care by experience users.
 - Novel implementation with external AMR package (AMReX) is underway for AMR EM-PIC: WarpX.



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