

20. Lecture #07
Spring 2016

Injectors

Ideally want distribution of monoenergetic particles with high current density and minimal phase-space size.

Source bias V_0

$\rho = \text{particle charge}$

$m = \text{particle mass}$

$R = \text{Radius/Aperture}$

$d = \text{Anode-Cathode Separation}$

Accelerator

Accelerating Gradient Options

Ions

Extraction Electrode

Plasma

Electron Gun

Drift Tube

Plasma

Anode

Cathode

Thermionic Emitter

Beam Pipe

Limiting Surface (PLASMA SHEATH OR MEANINGLESS)

B_{\perp}

V_0

ρ

m

R

d

Electrons

Emitted from filament tail of Fermi-Darrieus distribution of conduction electrons with current density

$$J = A T^2 e^{-W/kT}$$

Richardson-Dushman Eqn (1921)
Phil. Mag. 33 (1921)
Phys. Rev. 21 (1923)

$T = \text{cathode temp.}$

$W = \text{work function (eV)}$

$A = \frac{W e m k^2}{h^3} = 1.2 \times 10^6 \frac{A}{cm^2 K^2}$

Photomultiplier

- In lab, A often $\sim 2x$ lower.
- Thermionic cathode fabrication difficult.
- Low W at high temp.
- Smooth surface

X-FEL

$J \sim 10^{-10} \frac{A}{cm^2}$

+ Photomultipliers (not covered)

Often used for short pulse e^- sources for X-FEL facilities and e^- -microscopes.

Ions

Generally more complex than electron sources.

Many different technologies

- Light ions
- Heavy ions (H^+)
- Negative ions (H^-)

Analyze a simple "hot plate" source with fluid equations to identify scales.

Model ions as a cold fluid

$n(z,t) = \text{Density}$

$v(z,t) = \text{Flow Velocity}$

$\rho = \text{ion mass}$

$\rho = \text{ion charge}$

$\nabla \cdot \vec{v} = \text{Flow Velocity}$

$\text{Charge Conservation}$

$\frac{\partial n}{\partial t} + \nabla \cdot \vec{v} = 0$

$\frac{\partial v}{\partial t} + \frac{d}{dt}(n v_z) = 0$

$\Rightarrow \frac{\partial n}{\partial t} + \frac{d}{dt}(n v_z) = 0$

Momentum (Navier-Stokes + Cold Fluid)

$n \frac{d}{dt}(\rho \vec{v}) = \rho n \left(\vec{E} + \vec{V} \times \vec{B} \right) - \nabla(P) - \rho n \mu \nabla^2 \vec{v}$

Conductive Drift

$\vec{v}_{\text{comp}} = \frac{1}{2} \vec{B} \times \vec{E}$

No Pressure

$\rho = \text{constant}$

$\frac{\partial v_z}{\partial t} + n v_z \frac{\partial v_z}{\partial z} = \rho / E_z$

Force Equation

$E_z = \frac{P}{\rho v_z}$

$\frac{\partial v_z}{\partial z} = -\frac{P}{\rho v_z^2}$

Poisson Equation

Analyze currents assuming steady state = 0

1) Continuity Equation

$$\frac{\partial n}{\partial t} + \frac{\partial}{\partial z}(n v_z) = 0 \Rightarrow J = n v_z = \text{const} = J_0$$

Notice this implies $n \rightarrow 0$ as $z \rightarrow 0$. This is ok if current is still carried very long before it ends.

2) Force Equation

$$m \frac{\partial v_z}{\partial z} + n v_z \frac{\partial}{\partial z}(n v_z) = \rho F_{\text{ext}} = -\frac{\partial P}{\partial z}$$

$$\frac{1}{2} m v_z^2 + \frac{\partial}{\partial z}(n v_z)^2 = \rho F_{\text{ext}} = -\frac{\partial P}{\partial z}$$

$$V(z) \gg 0 \Rightarrow \text{profile carried over rest.}$$

$$\frac{1}{2} m v_z^2 = \rho V_0 \Rightarrow \frac{1}{2} m v_z^2 = \rho \frac{V_0}{L} (z - L)$$

Poisson Equation

$$\frac{\partial^2 \phi}{\partial z^2} = -\frac{n e}{\epsilon_0 (2 m)} \Rightarrow \frac{\partial^2 \phi}{\partial z^2} = \frac{20}{\epsilon_0 (2 m)} = \frac{J_0}{\epsilon_0 (2 m)} \frac{1}{z^2} \Rightarrow \frac{\partial \phi}{\partial z} = \frac{J_0}{\epsilon_0 (2 m)} z^{-1}$$

$$\frac{\partial \phi}{\partial z} = \frac{J_0}{\epsilon_0 (2 m)} z^{-1} \Rightarrow \frac{\partial \phi}{\partial z} = \frac{J_0}{\epsilon_0 (2 m)} z^{-1} \Rightarrow \frac{\partial \phi}{\partial z} = \frac{J_0}{\epsilon_0 (2 m)} z^{-1} \Rightarrow \frac{\partial \phi}{\partial z} = \frac{J_0}{\epsilon_0 (2 m)} z^{-1}$$

$$\Rightarrow \frac{\partial}{\partial z} \left[\frac{1}{2} \left(\frac{\partial \phi}{\partial z} \right)^2 \right] = \frac{J_0}{\epsilon_0 (2 m)} \frac{\partial}{\partial z} \left(\frac{\partial \phi}{\partial z} \right) \Rightarrow \frac{1}{2} \left(\frac{\partial \phi}{\partial z} \right)^2 = \frac{J_0^2}{\epsilon_0 (2 m)^2} z^{-2}$$

But

$$\frac{\partial \phi}{\partial z}(z=0) = V_0 - \rho v_z(0) = 0$$

$$\frac{\partial \phi}{\partial z}(z=L) = -\frac{J_0}{\epsilon_0 (2 m)} L = E_L(0) = 0$$

Space-Charge Limited Current

Limited current due to self space charge build up resulting in zero current before breakdown.

$$\Rightarrow \frac{J_0}{\epsilon_0 (2 m)} = \frac{(1/L)^{1/2}}{(\rho v_z)^{1/2}} \frac{L^{1/2}}{1^{1/2}}$$

Note that: $\frac{V_0}{d^2} \sim \begin{cases} V_0^{-1/2} & d \leq 1 \text{ cm} \\ V_0^{-5/4} & d > 1 \text{ cm} \end{cases}$

$$I = \text{const} \frac{V_0^{3/2}}{d^2} \sim \frac{V_0^{3/2}}{d^5} \sim \frac{V_0}{d^{5/4}}$$

$$R \sim d$$

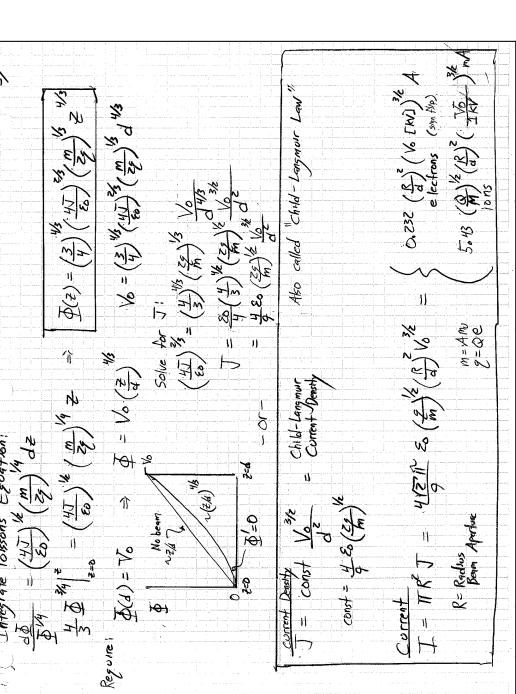
• I increases as source size increases

Also want sources that deliver maximum current in place-space volume measures of the beam.

Will find later that normalized rms x- and y- components measure \perp phase-space terms of the beam:

$$\begin{aligned} E_{nx} &= \langle \partial p [x^2 x' x'^2] - \langle x \rangle \langle x' \rangle^2 \rangle^{1/2} \\ E_{ny} &= \langle \partial p [y^2 y' y'^2] - \langle y \rangle \langle y' \rangle^2 \rangle^{1/2} \end{aligned}$$

Phase-Space $\sim E_{nx} E_{ny}$
Volume



$$\begin{aligned} \text{Current} &= \pi R^2 V_0 \frac{3/2}{d^2} = \pi R^2 V_0 \frac{1/2}{d^5} = \frac{4\pi R^2}{9} \left(\frac{V_0}{d} \right)^{1/2} A \\ I &= \pi R^2 V_0 \frac{3/2}{d^2} = \frac{4\pi R^2}{9} \left(\frac{V_0}{d} \right)^{1/2} A \\ R &= \text{Radius Aperture} \\ m = A n & \\ Z = \text{arc} & \end{aligned}$$

6) Want for source: $J = \text{const} \propto V_0^{3/2} / d^2$

J high $\Rightarrow V_0$ large $\Rightarrow d$ small

But must also suppose:

1) Voltage Breakdown

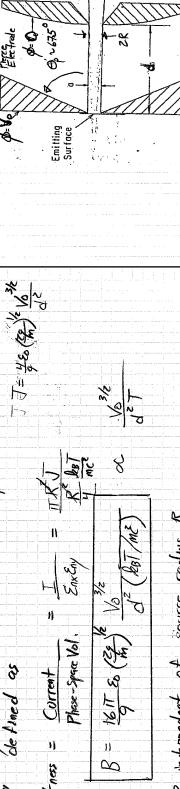
$$V_0 \propto 100 \text{ kV} \quad \begin{cases} \left(\frac{d}{\text{cm}} \right) & \text{for } d \leq 1 \text{ cm} \\ \left(\frac{d}{\text{cm}} \right)^{1/2} & \text{for } d > 1 \text{ cm} \end{cases}$$

Subject to avoid distortion of hardware

2) Optical Aberrations

Non-linear fields must be suppressed to preserve good beam quality,
Real Beam 3D not 1D

Find angled "Pierce Electrodes" can be used to keep beam approx 1D. But even with detailed code of optimization, And must have



R = beam aperture radius.

Note: B independent of source radius R

Want ions at low a temp T as possible!

Had to do

AT Formulas
Wiley, 1988

Summary: Sources

- o Well functioning sources crucial for accelerator:
 - Bright: compact place - space \Leftrightarrow compact beam
 - smaller (more economical) structures
 - lower losses to mitigate damage
 - Improving sources allows running higher for intensity to get more out of accelerator.
 - Upgrade source \Leftrightarrow Upgrade accelerator
- o Need also high reliability for long periods of time
 - Source not operational, then expensive machine will not work!
- o Sources high brightness, but also difficult!
 - Technology and physics strongly coupled
 - Rely on different material science, plasma physics etc.
- o Possible to focus a whole course on just one type of source technology,
- o Many types of sources. Only scratches surface in this lecture:

<u>Electrons</u>	<u>Ions</u>	<u>Radioactive</u>	<u>Antiprotons</u>
Thermionic emitters	hot plate (ion)	Capture cool	Alcohol driven source - capture, cool, inject
Field Emission (point)	plasma (beam)		
Photocathodes	ECR		
	laser driven		
	beam driven		
- o Source projects great for PhDs: rich physics, improvements high longage